

**Overall average treatment effects  
and one-variable-at-a-time  
subgroup analysis:  
The Scylla and Charybdis of  
Evidence Based Medicine**



**David M. Kent, MD, MSc**

Professor of Medicine, Neurology, Clinical and Translational Science,  
Director, Predictive Analytics and Comparative Effectiveness (PACE) Center,  
Institute for Clinical Research and Health Policy Studies, Tufts Medical Center

# Scylla and Charybdis



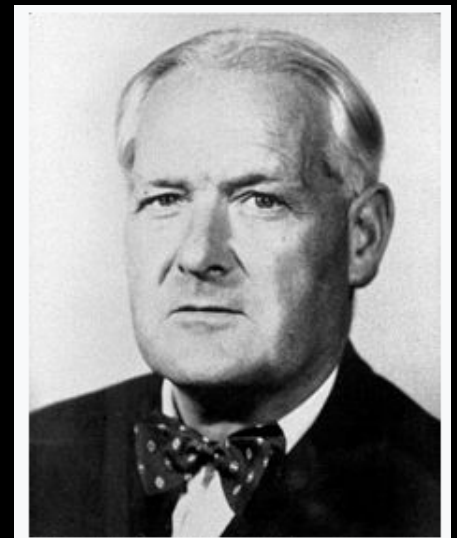
Overall trial results

One-variable-at-time  
subgroup analysis

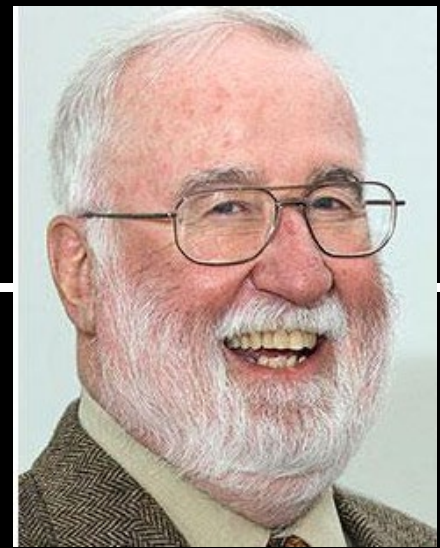
# Limitations of RCTs for Clinical Decision Making

# Limitations of RCTs for Clinical Decision Making

- While RCTs can determine the better treatment on average, they “do not answer the practicing doctor's question: *what is the most likely outcome when this particular drug is given to a particular patient?*”
  - Austin Bradford Hill



# Evidence Based Medicine



- Hill was wrong.
- RCTs should be used by doctors to determine what's best for individual patients.
- "Evidence based medicine is the conscientious, explicit, judicious and reasonable use of current best evidence in making decisions about the care of individual patients."

- EBM proposed to repurpose RCTs from tools to establish causation into tools for *prediction* in single cases.

- What's best on average must be best for each individual.

# The Fallacy of Division (Wennington's Fallacy)



Starters	PTS
<a href="#">B.J. Armstrong</a>	16
<a href="#">Scottie Pippen</a>	19
<a href="#">Michael Jordan</a>	55
<a href="#">Toni Kukoc</a>	3
<a href="#">Will Perdue</a>	6
Reserves	PTS
<a href="#">Luc Longley</a>	5
<a href="#">Corie Blount</a>	2
<a href="#">Steve Kerr</a>	5
<a href="#">Larry Krystkowiak</a>	0
<a href="#">Bill Wennington</a>	2
<a href="#">Pete Myers</a>	0
<b>Team Totals</b>	<b>113</b>

*“Michael and I combined for 57 points”*

*-Bill Wennington, 1995*



- It is potentially misleading to draw inferences about individuals based on aggregated characteristics of the (heterogeneous) group to which they belong.
- How do we estimate “individual” treatment effects?

# Clinical Trial: "Box Score"

■ ACTUAL OUTCOME

0 = alive

1 = dead

Individual Treatment Effects in a  
Deterministic Framework: Four  
possibilities

Without Treatment	With Treatment	
0	0	NO EFFECT
0	1	<b>HARM</b>
1	0	<b>BENEFIT</b>
1	1	NO EFFECT

Subject Name	Without Treatment	With Treatment
SAM	0	
MARY		0
BOB	0	
BEN		0
CHRISTINE		0
NEIL	1	
MOHAMED		1
JENNIFER		1
PAUL	0	
NISHA	1	
MIGUEL	1	
LAYLA		0
PAUL	0	
EMANUEL		1
CHERYL		0
PATRICK	0	
OSCAR		1
JULIANNE	0	
THOMAS	0	
GEORGE		0

# Clinical Trial: "Box Score"

■ ACTUAL OUTCOME  
■ COUNTER FACTUAL OUTCOME

0 = alive  
 1 = dead

Individual Treatment Effects in a Deterministic Framework: Four possibilities

Without Treatment	With Treatment	
0	0	NO EFFECT
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Subject Name	Without Treatment	With Treatment
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MARY	0	0
BOB	0	0
BEN	1	0
CHRISTINE	1	0
NEIL	1	1
MOHAMED	1	1
JENNIFER	1	1
PAUL	0	1
NISHA	1	1
MIGUEL	1	1
LAYLA	1	0
PAUL	0	0
EMANUEL	1	1
CHERYL	0	0
PATRICK	0	0
OSCAR	1	1
JULIANNE	0	0
THOMAS	0	0
GEORGE	1	0

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EMANUEL	1	1
CHERYL	0	0
PATRICK	0	0
OSCAR	1	1
JULIANNE	0	0
THOMAS	0	0
GEORGE	1	0

← HARM

← BENEFIT

← BENEFIT

← HARM

← BENEFIT

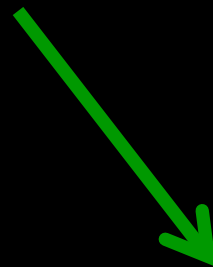
← BENEFIT

# Clinical Trial: "Box Score"

0 = alive  
1 = dead

Without Treatment	With Treatment
0	1
0	0
0	0
1	0
1	0
1	1
1	1
1	1
1	1
0	1
1	1
1	1
1	0
0	0
1	1
0	0
0	0
1	1
0	0
0	0
1	0

**BENEFIT**



<b>Proportion Dead</b>	<b>11/20 (55%)</b>	<b>9/20 (45%)</b>
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# Conventional Approach: One variable at a time subgroup analysis

- This approach relies on the detection of “statistically significant” effect modifiers—contrasting *relative* treatment effects across levels of each subgrouping variable, one-variable-at-a-time.

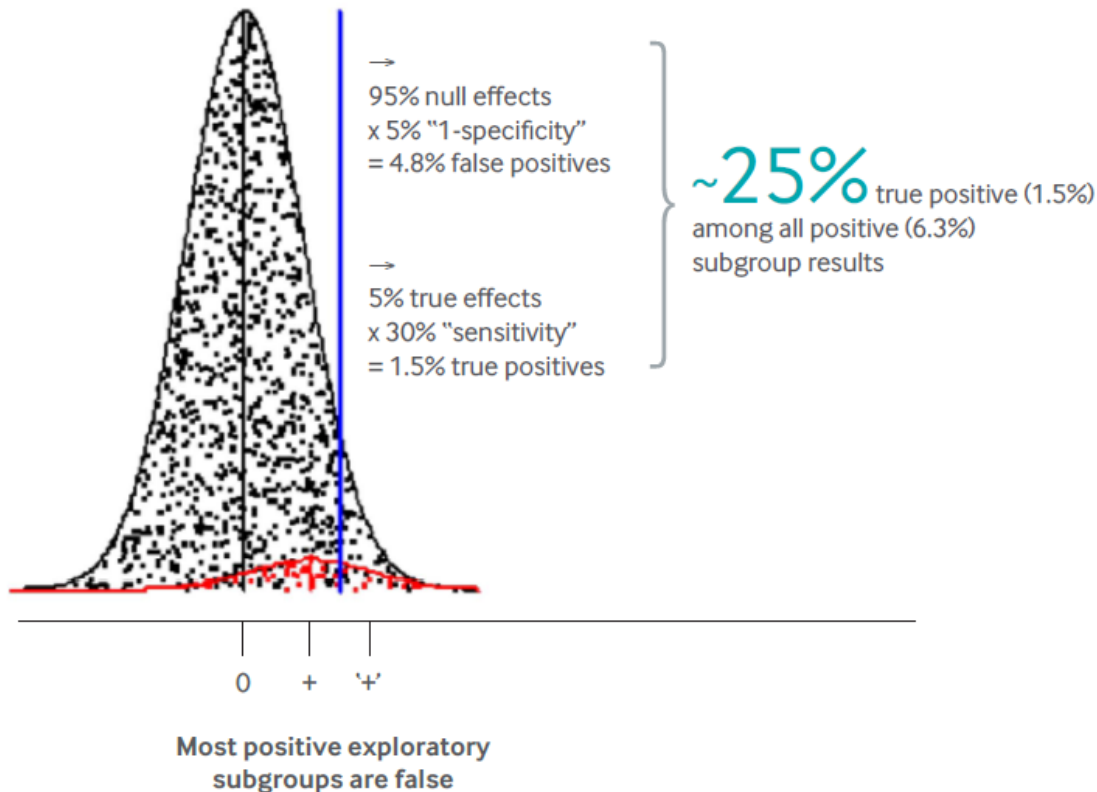
# Problems With Conventional Subgroup Analysis

- **Fail to detect HTE even when its there:**
  - **Low power**
    - For covariates with 50% prevalence (e.g. gender): ~4 fold the sample size.
    - For covariates with 20% prevalence (e.g. common comorbidities): ~10 fold the sample size.
  - **Compare Groups of patients that are more similar than dissimilar.**
- **Individuals patients belong to many different subgroups.**
- **Spurious False Positives**

# Why most subgroup effects are false or overestimated

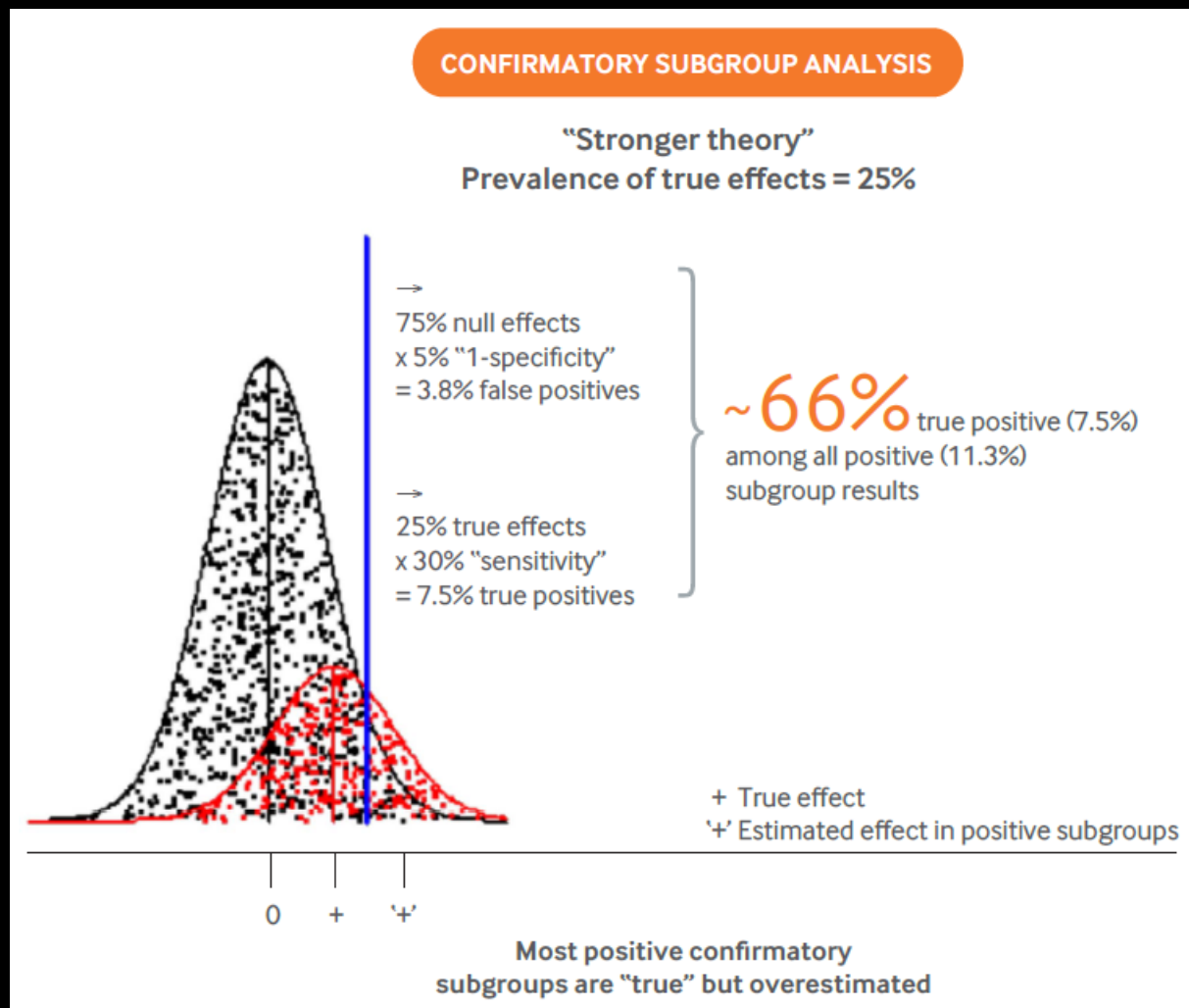
## EXPLORATORY SUBGROUP ANALYSIS

Weak theory and noisy data  
Prevalence of true effects = 5%





# Why most subgroup effects are false or overestimated



# “Positive” subgroup analyses subsequently shown to be false

Observation	Refutation
Aspirin is ineffective in secondary prevention of stroke in women <sup>29,30</sup>	31

# Interim Summary

- Determining the best treatment on average (the task of an RCT) is very different from determining the best treatment for an individual (the task of a good clinician) .
- Conventional subgroup analysis of clinical trials are typically inadequate and can also be misleading, and are not consistent with the clinically most important goal of *prediction*.

- The reference class problem is a model selection problem
- The goal of Personalized EBM can be conceived as the identification of an optimal subgrouping scheme, based on all relevant patient characteristics, that yields a more individualized reference class for each patient than the overall trial results.

# Why Risk Based Subgroup Analysis Should be Routine



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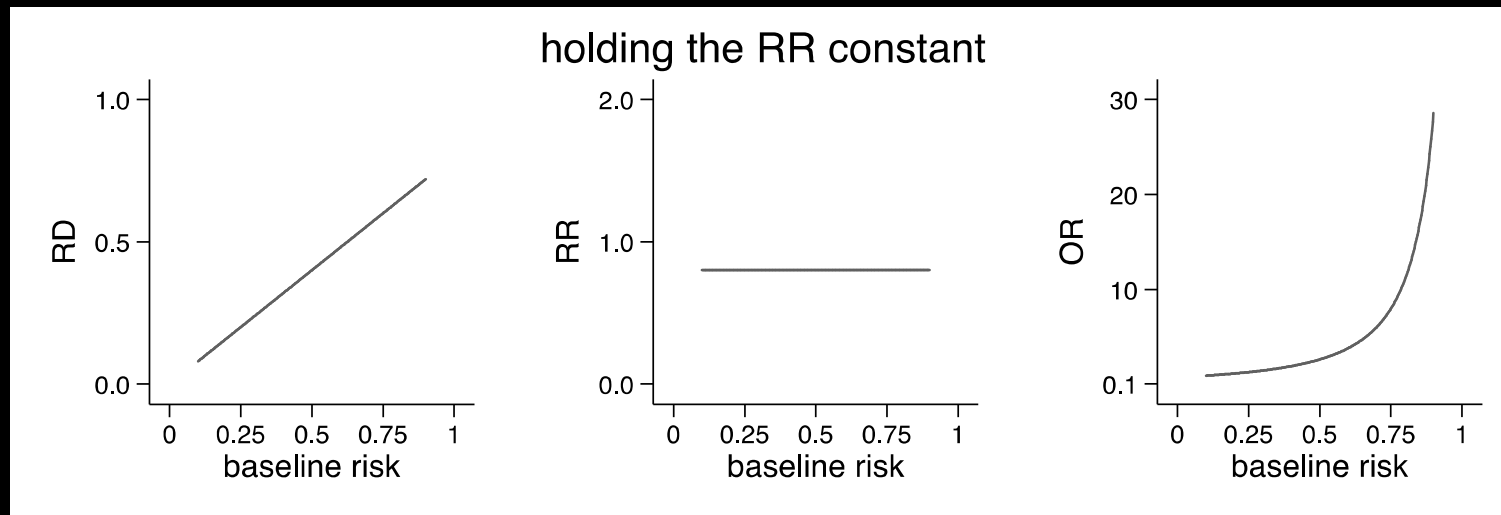
# Why privilege risk-based HTE analysis?

- Risk is a known mathematical determinant of treatment effect.

# Common Measures of Treatment Effect

Risk Reduction (RR)	Definition
Absolute RR	$EER - CER$
Relative RR	$1 - \frac{EER}{CER}$
Odds Ratio	$\frac{EER / (1 - EER)}{CER / (1 - CER)}$
<i>CER</i> =control event rate <i>EER</i> =experimental event rate	

# An Illustration of Scale Dependence of HTE over Baseline Outcome Risk



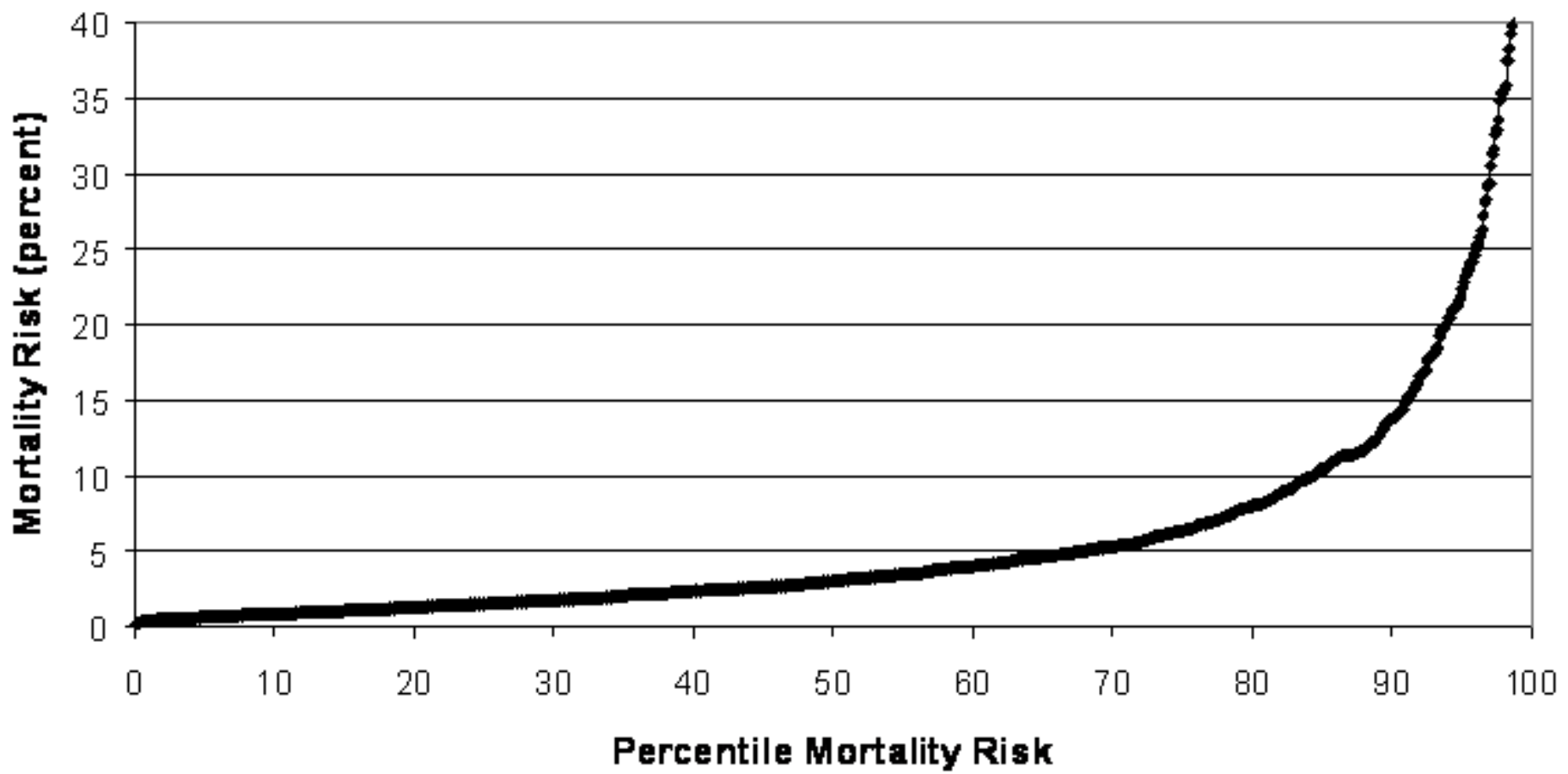
Dahabreh, Hayward, Kent, IJE, 2016



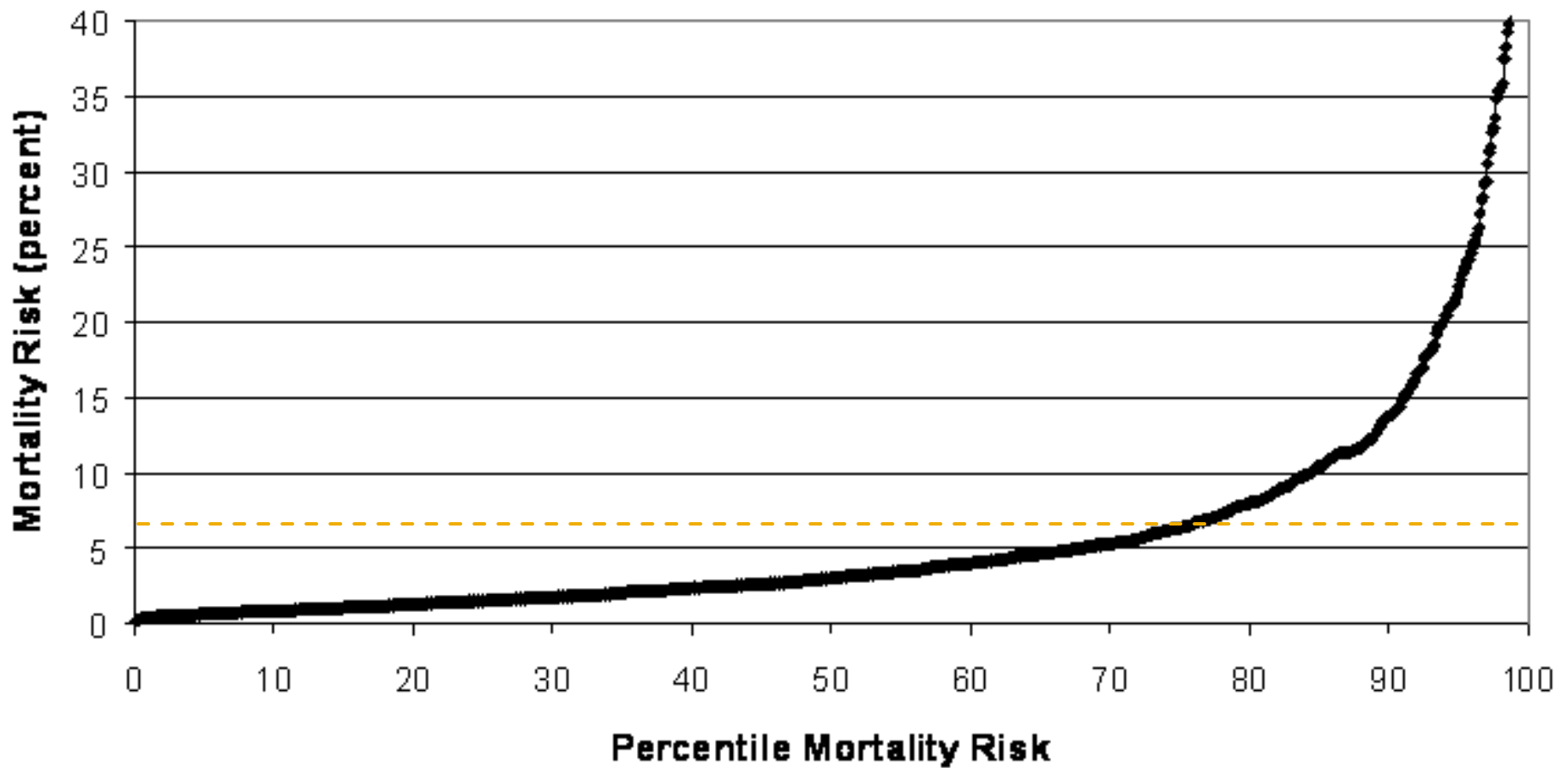
# Why privilege risk-based HTE analysis?

- Risk is a known mathematical determinant of treatment effect.
- When baseline risk heterogeneity is present (and the treatment effect is non-zero), there is always HTE.
- Risk provides a summary measure that takes into account multiple variables that are relevant; provides “patient-centered” evidence.

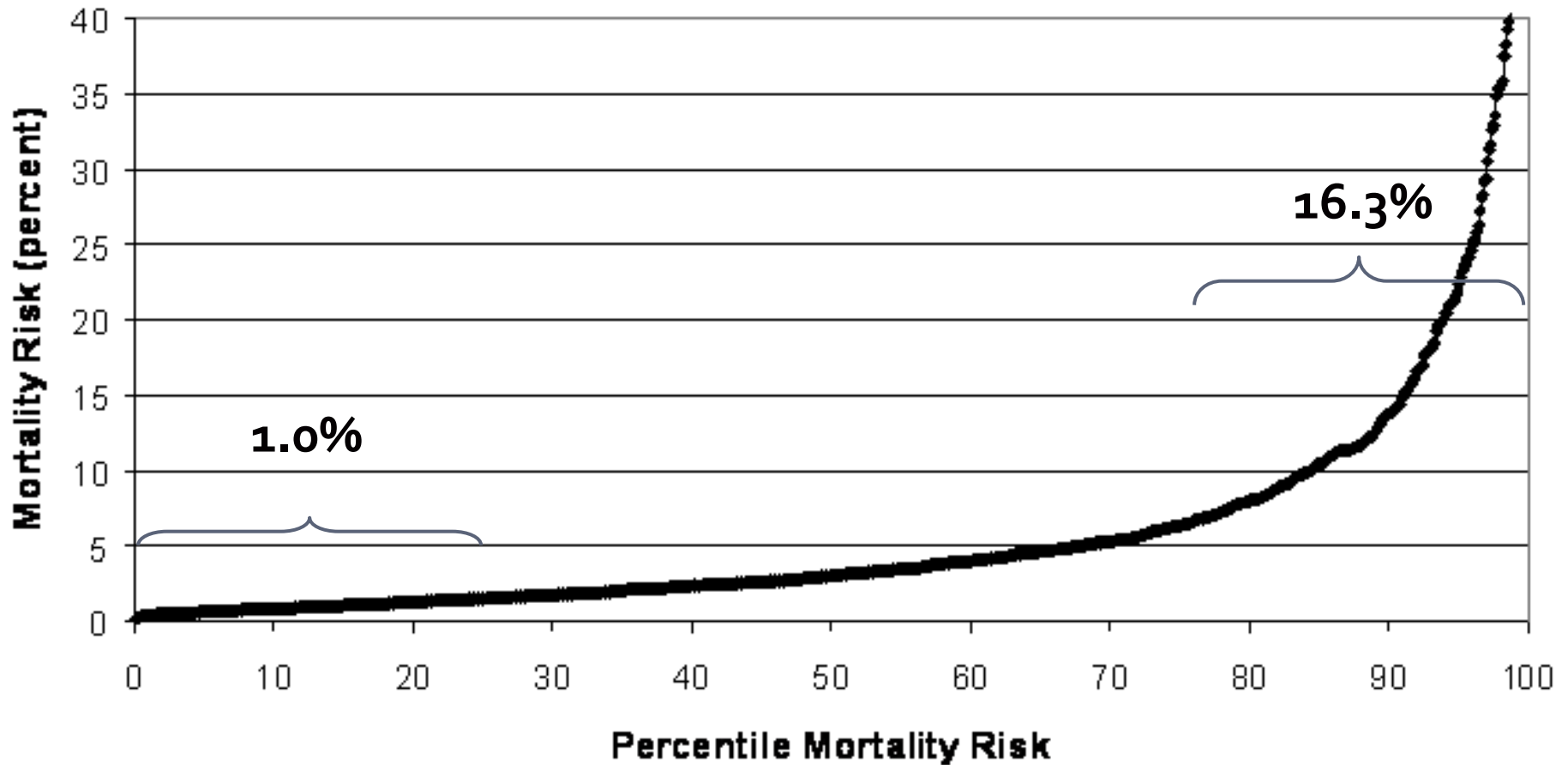
**Figure 1: Distribution of Mortality Risk with Thrombolytic Therapy in Patients with Acute Myocardial Infarction**



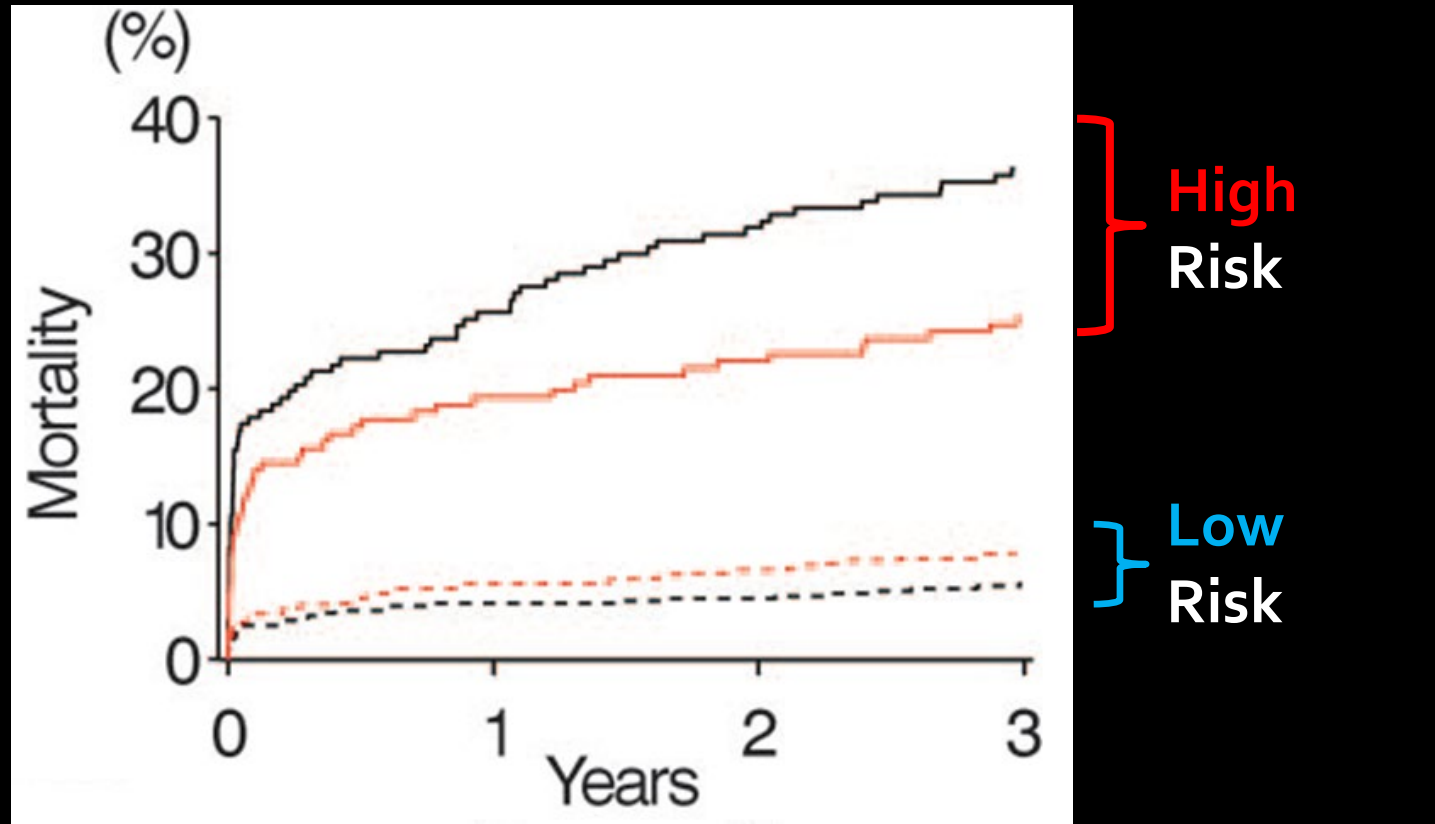
**Figure 1: Distribution of Mortality Risk with Thrombolytic Therapy in Patients with Acute Myocardial Infarction**



**Figure 1: Distribution of Mortality Risk with Thrombolytic Therapy in Patients with Acute Myocardial Infarction**



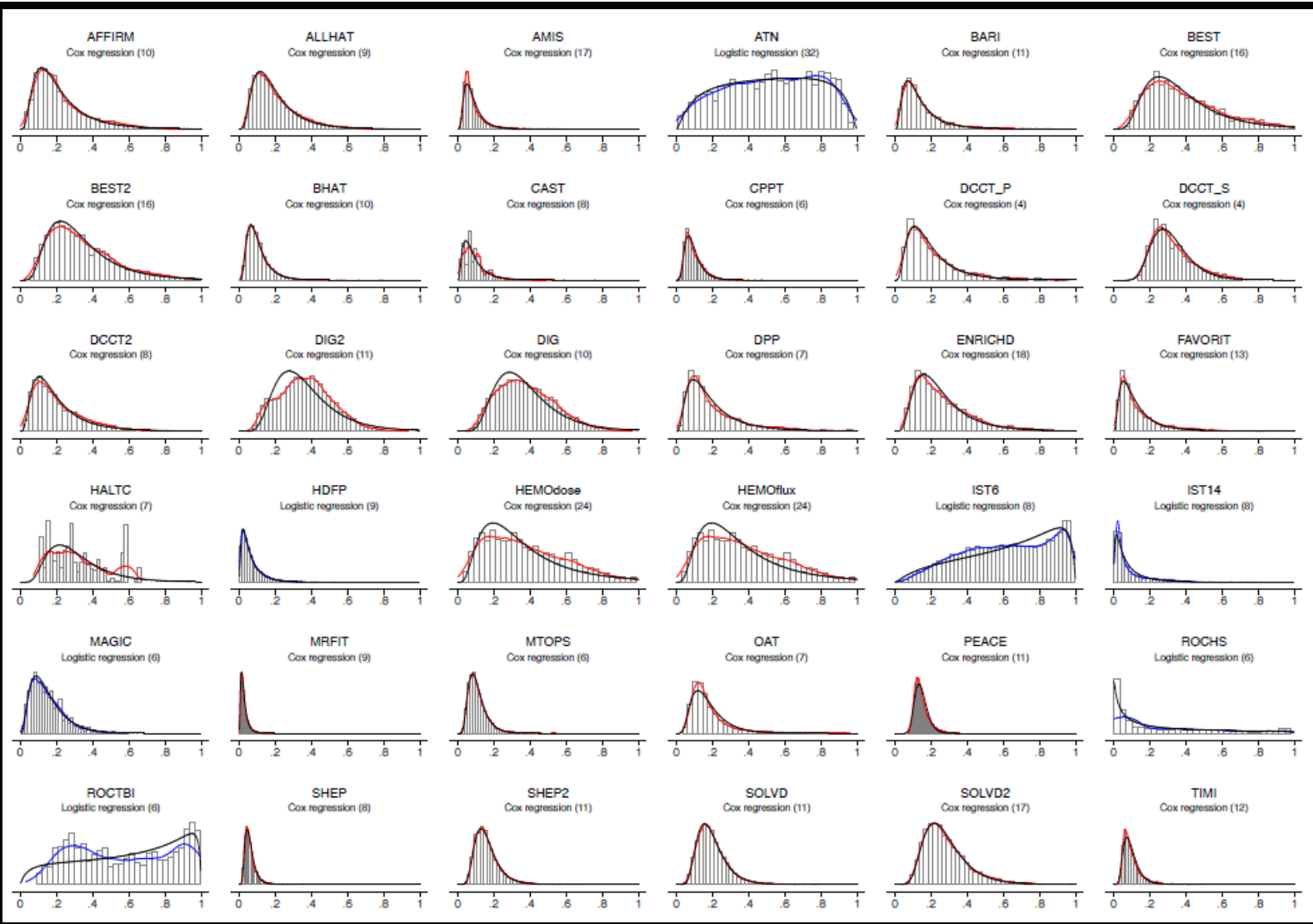
# DANAMI-2



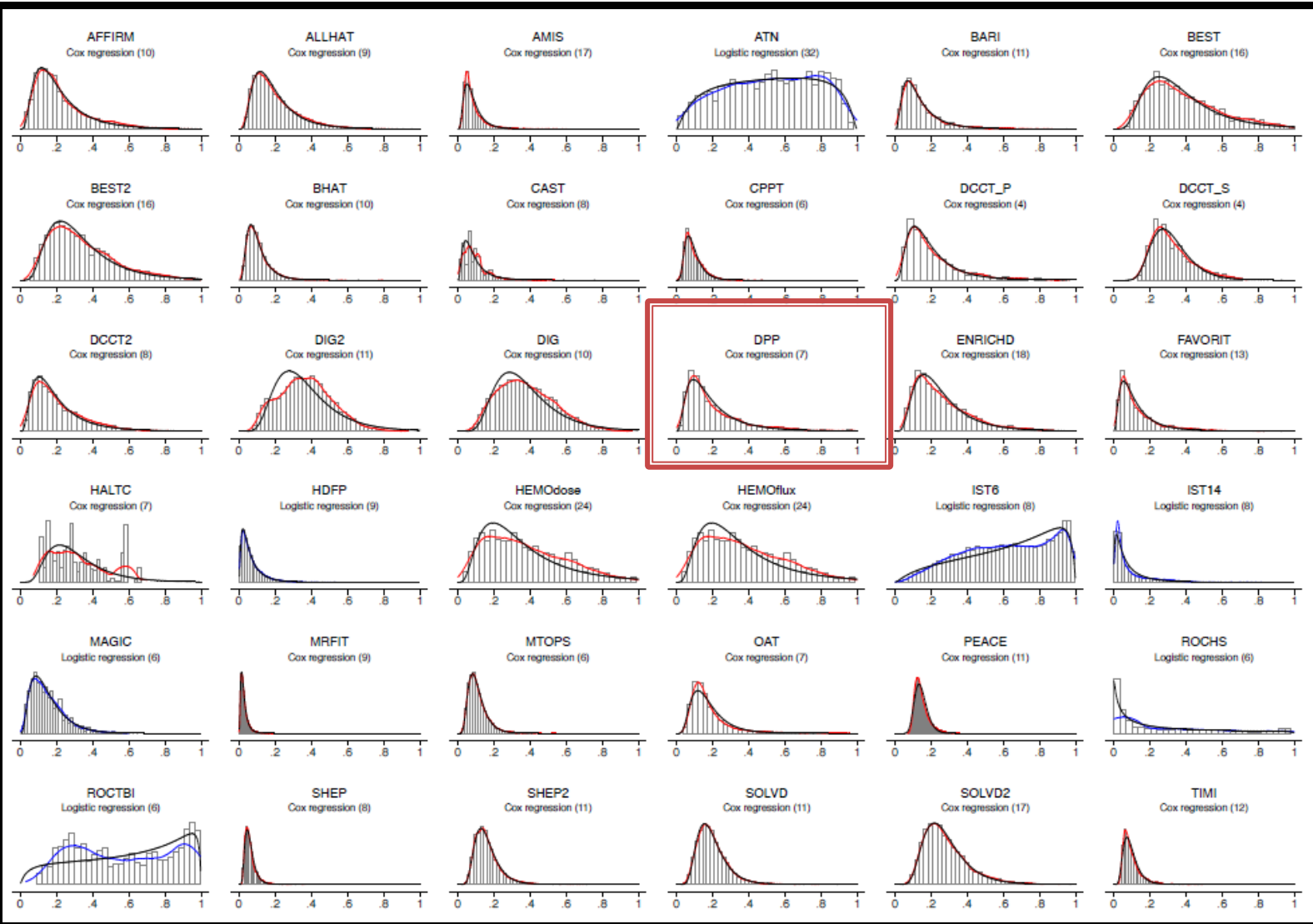
Number at risk				
TIMI 0-4	Fx	556	533	531
	PA	578	546	540
TIMI ≥ 5	Fx	207	154	141
	PA	186	150	145

— PCI  
— Medical Therapy

# Predicted Risk Distributions in RCTs



# Predicted Risk Distributions in RCTs



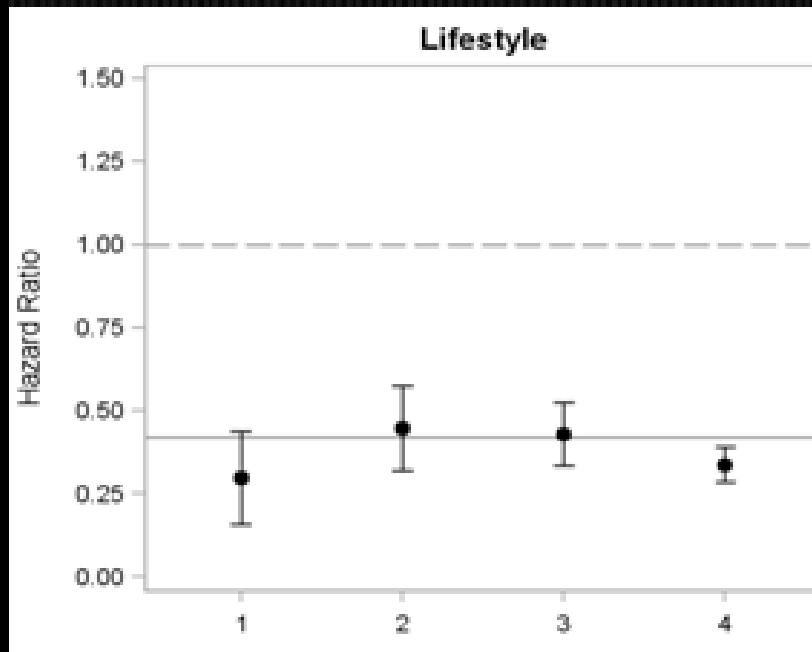
# Diabetes Prevention Program (DPP) Randomized Controlled Trial

- Participants: 3060 nondiabetic persons with evidence of impaired glucose metabolism.
- Intervention: Intervention groups received metformin or a lifestyle-modification program.
- Main Outcome Measure: Development of diabetes

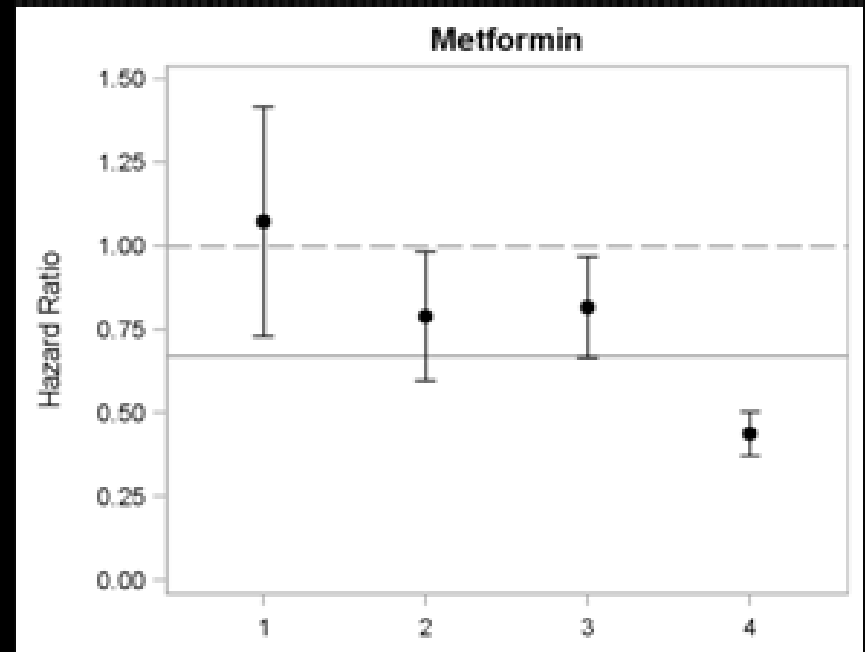
*The DPP study was conducted by the DPP Investigators and supported by the National Institute of Diabetes and Digestive and Kidney Diseases (NIDDK).*



# DPP Risk Stratified Results

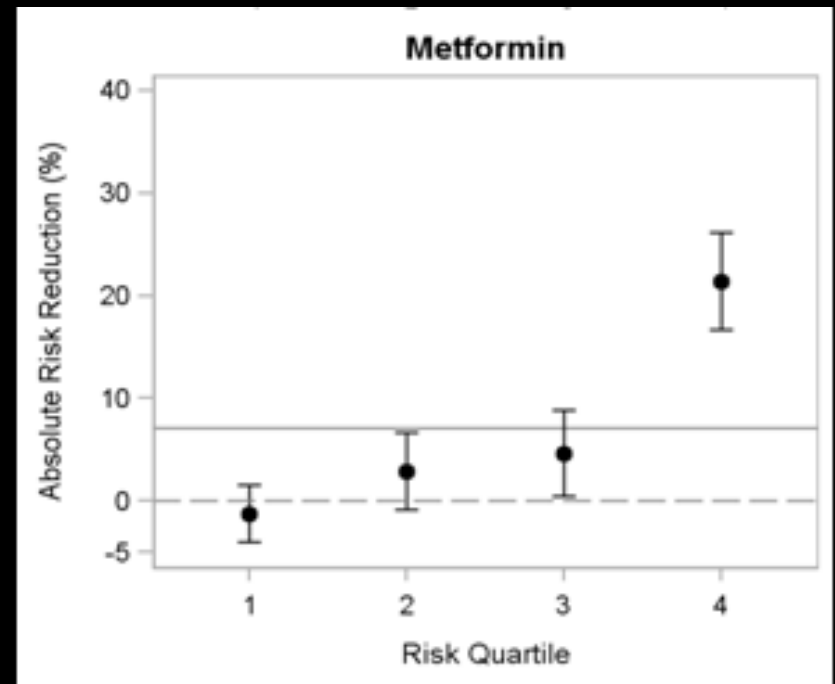
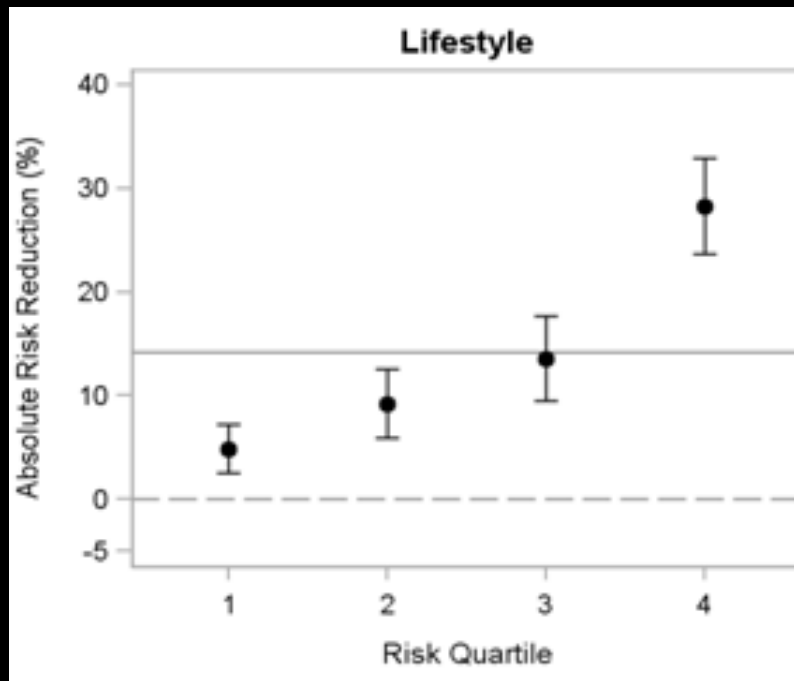


p value = NS



p value = 0.0008

# DPP Risk Stratified Results



# Risk based analyses can reveal counter-intuitive findings

- Overall effectiveness results may be driven by a relatively small group of influential (typically high risk) patients;
- The typical (median) risk patient is frequently at considerably lower risk than the overall average;
- The average benefit seen in the summary result often over estimates the benefit (on the RD scale) in most patients (and may obscure harm in many).

# Assessing and reporting heterogeneity in treatment effects in clinical trials: a proposal



David M Kent<sup>1\*</sup>, Peter M Rothwell<sup>2</sup>, John PA Ioannidis<sup>1,3</sup>, Doug G Altman<sup>4</sup>, Rodney A Hayward<sup>5</sup>

1. Evaluate and **report on the distribution of risk** in the overall study population and in the separate treatment arms of the study by using a risk prediction model or index.
2. Primary subgroup analyses should include reporting how relative and absolute risk reduction varies in a **risk-stratified analysis**.
3. Any additional **primary subgroup analysis should be pre-specified** and limited to patient attributes with strong a prior pathophysiological or empirical justification.
4. Conduct and **report on secondary (exploratory) subgroup analyses separate** from primary subgroup comparisons.
5. All analyses conducted must be reported and statistical testing of HTE should be done using **appropriate methods** (such as interaction terms) and avoiding over-interpretation.



thebmj

STATE OF THE ART REVIEW

Annals of Internal Medicine

The Predictive Approach Statement: Explanation of Heterogeneous Treatment Effects (HTE) in Clinical Decision Making

David M. Kent, MD, MS; David v Steve Goodman, MD, MHS, PhD; Michael Pencina, PhD; Gowri Andrew Vickers, PhD; John B

The PATH (Predictive Approach Statement) Statement was developed to provide guidance for predictive treatment effects (HTE) in clinical decision making. HTE analysis is to provide patient-centered risk with versus without the intervention, taking relevant patient attributes simultaneously, to support personalized clinical decision making than can be made on the basis of only an overall average treatment effect. The authors distinguished 2 categories of predictive HTE approaches (a "risk-modeling" and an "effect-modeling" approach) and developed 4 sets of guidance statements: criteria to determine when risk-modeling approaches are likely to identify clinically meaningful

THE LEARNING HEALTH SYSTEM SERIES

CARING FOR THE INDIVIDUAL PATIENT

Understanding Heterogeneous Treatment Effects

David Kent, Jessica Paulus, Mahnoor Ahmed, and Danielle Whicher, Editors

NATIONAL ACADEMY OF MEDICINE

SUPPORTING METHODS

Heterogeneity

David Kent-Lake, MFS; Sally Morton, PhD; Ravi Varadhan, PhD

applied to disaggregate patients and an herein a model is developed on m for treatment assignment and and baseline covariates. Both dict differential absolute treat- ale for clinical decision making. guidance: criteria to determine are likely to identify clinically pects of risk-modeling meth- to clinical practice, and conse- use of effect-modeling app- together with its explanation ide future analyses and re-

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# Risk modeling vs. Effect modeling

Annals of Internal Medicine RESEARCH AND REPORTING METHODS

## The Predictive Approaches to Treatment effect Heterogeneity (PATH) Statement: Explanation and Elaboration

Table 2. Equations Corresponding to Risk-Modeling and Effect-Modeling Approaches

### Risk modeling

A multivariable regression model  $f$  that predicts the risk for an outcome based on risk predictors  $x_i$  is identified or developed:

**Equation 1:**  $risk = f(\alpha + \beta_1 \times x_1 + \dots + \beta_p \times x_p)$

Variation in the treatment effect across risk can be tested statistically on the relative scale through the interaction between a linear predictor of risk ( $lp = \beta_1 \times x_1 + \dots + \beta_p \times x_p$ ) and treatment assignment  $tx$ :

**Equation 2:**  $risk = f(\alpha + \beta_{tx} \times tx + \beta_{lp} \times lp + \delta_{lp} \times lp \times tx)$

Including a treatment interaction with the linear predictor of risk permits the relative treatment effect to vary linearly across levels of risk (and permits testing of the statistical significance of this interaction effect,  $\delta_{lp}$ ).

When relative effects across risk strata seem constant, a model with a constant treatment effect may suffice:

**Equation 3:**  $risk = f(\alpha + \beta_{tx} \times tx + \beta_1 \times x_1 + \dots + \beta_p \times x_p)$ ,

where the parameter  $\beta_{tx}$  represents a constant risk reduction on the log hazard or log odds scale for treated ( $tx = 1$ ) versus control ( $tx = 0$ ) patients.

### Effect modeling

A regression model  $f$  is developed on RCT data with inclusion of risk predictors  $x_i$ , a treatment assignment variable  $tx$ , and potential treatment interaction terms ( $x_i \times tx$ ):

**Equation 4:**  $risk = f(\alpha + \beta_{tx} \times tx + \beta_1 \times x_1 + \dots + \beta_p \times x_p + \delta_t \times x_1 \times tx + \dots + \delta_p \times x_p \times tx)$

RCT = randomized controlled trial.



## JAMA | Original Investigation

## Heterogeneity of Treatment Effects in an Analysis of Pooled Individual Patient Data From Randomized Trials of Device Closure of Patent Foramen Ovale After Stroke

David M. Kent, MD, MS; Jeffrey L. Saver, MD; Scott E. Kasner, MD; Jason Nelson, MS; John D. Carroll, MD; Gilles Chatellier, MD; Geneviève Derumeaux, MD; Anthony J. Furlan, MD; Howard C. Herrmann, MD; Peter Jüni, MD; Jong S. Kim, MD; Benjamin Koethe, MS; Pil Hyung Lee, MD; Benedicte Lefebvre, MD; Heinrich P. Mattle, MD; Bernhard Meier, MD; Mark Reisman, MD; Richard W. Smalling, MD, PhD; Lars Soendergaard, MD; Jae-Kwan Song, MD; Jean-Louis Mas, MD; David E. Thaler, MD, PhD

**IMPORTANCE** Patent foramen ovale (PFO)-associated strokes comprise approximately 10% of ischemic strokes in adults aged 18 to 60 years. While device closure decreases stroke recurrence risk overall, the best treatment for any individual is often unclear.

**OBJECTIVE** To evaluate heterogeneity of treatment effect of PFO closure on stroke recurrence based on previously developed scoring systems.

**DESIGN, SETTING, AND PARTICIPANTS** Investigators for the Systematic, Collaborative, PFO Closure Evaluation (SCOPE) Consortium pooled individual patient data from all 6 randomized clinical trials that compared PFO closure plus medical therapy vs medical therapy alone in patients with PFO-associated stroke, and included a total of 3740 participants. The trials were conducted worldwide from 2000 to 2017.

**EXPOSURES** PFO closure plus medical therapy vs medical therapy alone. Subgroup analyses used the Risk of Paradoxical Embolism (RoPE) Score (a 10-point scoring system in which higher scores reflect younger age and the absence of vascular risk factors) and the PFO-Associated Stroke Causal Likelihood (PASCAL) Classification System, which combines the RoPE Score with high-risk PFO features (either an atrial septal aneurysm or a large-sized shunt) to classify patients into 3 categories of causal relatedness: unlikely, possible,

## Redevelopment and validation of a strategy to individualise decision making for surgical revascularisation in patients with complex coronary artery disease: second randomised controlled trial

Kuniaki Takahashi, Patrick W Serruys, Valentin Fuster, Jung-Min Ahn, Arie Pieter Kappetein, Stuart J Head, David van Klaveren, on behalf of the SYNTAXES, FREEL

### Summary

**Background** Randomised controlled trials of percutaneous coronary interventions, and typically report the average effect of an intervention compared with medical therapy. However, the effect may vary between patients, basing treatment decisions on average may be suboptimal. We aimed to develop an individualised treatment strategy in patients with complex coronary artery disease.

- [← Editorial page 2265](#)
- [← Related article page 2312](#)
- [+ Supplemental content](#)
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# Summary

- Heterogeneity of outcome risk is ubiquitous.
- Heterogeneity of outcome risk inevitably gives rise to heterogeneity of treatment effect.
- One variable at a time subgroup analyses are inadequate (and prone to spurious false positive results).
- Risk based subgroup analyses can do better.



